# Imperial College London

## **MODULE 3 CLASS**

Aidan Hogg & Patrick Naylor - Autumn Term 2020 ELEC50013: Signal and Systems Department of Electrical and Electronic Engineering

#### Method:

- 1: Conceptual question posed students individually come up initial answer **(5 mins)**
- 2: Explanation/discussion of correct answer (5 mins)

What is the effect on the frequency spectrum if a continuous signal x(t) is sampled?

- A: The spectrum becomes periodic
- B: The spectrum becomes real
- C: The spectrum becomes periodic and real
- D: The spectrum becomes periodic and symmetric

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One Domain	Other Domain
Discrete	Periodic
Symmetric	Symmetric
Antisymmetric	Antisymmetric
Real	Conjugate Symmetric
Imaginary	Conjugate Antisymmetric
Real & Symmetric	Real & Symmetric
Real & Antisymmetric	Imaginary & Antisymmetric

# What is the sampling frequency that would satisfy the Nyquist Sampling Criterion of the signal:

 $x(t) = 5 + \cos(4000\pi t) + \sin(8000\pi t)$ 

- A:  $f_s > 4000 \text{ Hz}$
- B:  $f_s > 12000 \text{ Hz}$
- C:  $f_s > 8000 \ \mathrm{Hz}$
- D:  $f_s > \rm 16000\ Hz$

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Given

$$x(t) = 5 + \cos(4000\pi t) + \sin(8000\pi t)$$

Highest frequency component in 5 is 0Hz Highest frequency component in  $\cos(4000\pi t)$  is  $\omega = 4000\pi$ Highest frequency component in  $\sin(8000\pi t)$  is  $\omega = 8000\pi$ 

So the maximum frequency component in x(t) is  $\omega = 8000\pi$ 

$$\therefore \quad 2\pi f = 8000\pi \qquad \therefore \quad f = 4000$$

Nyquist Sampling Criterion,  $f_s > 2f = 8000 \text{ Hz}$ 

A sine wave of frequency f is sampled 8 times at a sampling frequency of  $f_s$ .



If the plot shows the magnitude response of the 8 samples what were the values of f and  $f_s$ ?

A: f = 2000Hz  $f_s = 16000$ Hz B: f = 1000Hz  $f_s = 6000$ Hz C: f = 15000Hz  $f_s = 12000$ Hz A sine wave of frequency f is sampled 8 times at a sampling frequency of  $f_s$ .



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#### **EXPLANATION**

A: 
$$f = 2000$$
Hz  $f_s = 16000$ Hz

B: f = 1000Hz  $f_s = 6000$ Hz

C: f = 15000Hz  $f_s = 12000$ Hz



Effect of aliasing in the frequency domain

It is now common practice to process analog signals digitally:



### What is the purpose of B?

- A: A low pass filter to remove spectral images
- B: A low pass filter to prevent aliasing
- C: A high pass filter to remove spectral images
- D: A high pass filter to prevent aliasing

#### It is now common practice to process analog signals digitally:



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- A: A low pass filter to remove spectral images
- B: A low pass filter to prevent aliasing
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Which of these statements are true? (multiple options allowed)

Oversampling is used because...

- A: ...it relaxes the requirements of the anti-aliasing filter
- B: ...it relaxes the requirements of the anti-imaging filter
- C: ...it reduces the computational complexity and the cost

Which of these statements are true? (multiple options allowed)

Oversampling is used because...

- A: ...it relaxes the requirements of the anti-aliasing filter
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## **QUESTION 6:**

## Which row shows the process of quantization?



#### ANSWER

## Which row shows the process of quantization?





#### Quantization

(only 1 bits to represent all the colours)

## Undersampling

(fewer pixels available to represent the image)

## High-pass Filtering

(detects edges in the image)